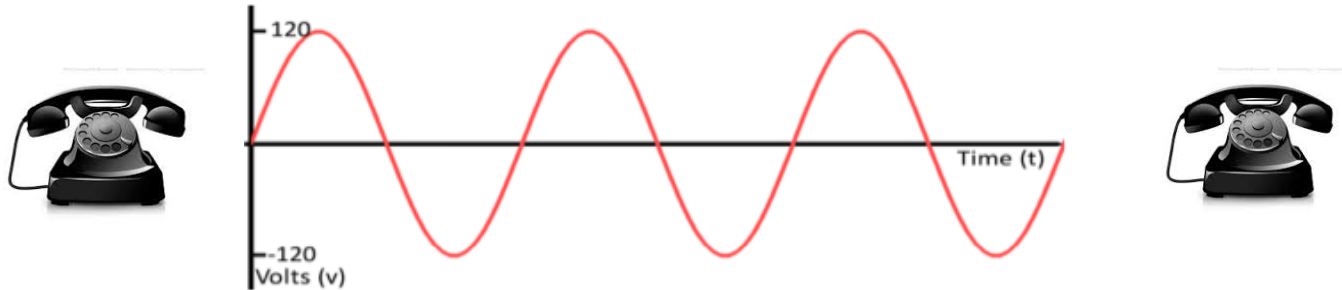


# Bits, Bytes, Ints

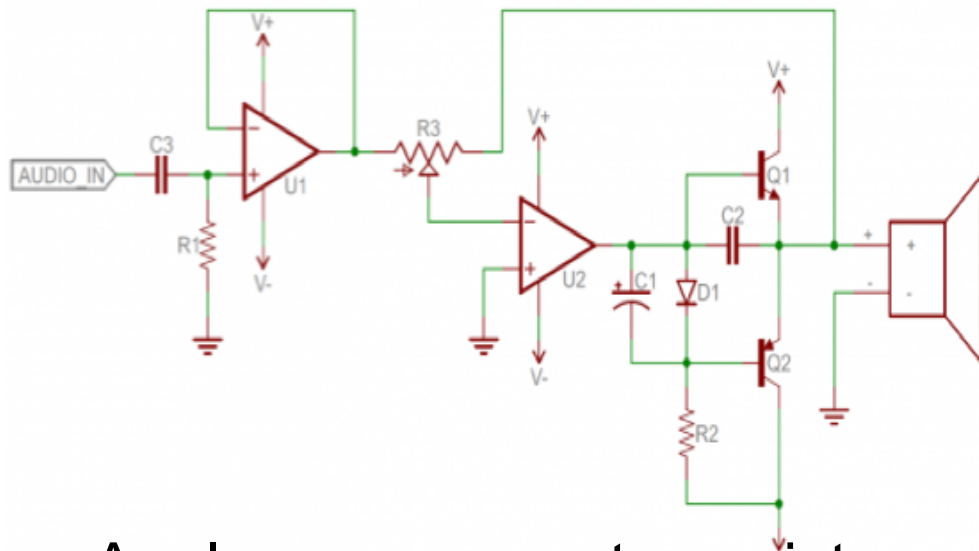
Shuai Mu

Slides are based on Tiger Wang's and Jinyang Li's class

# The world has moved away from analog signal to ...



Analog signals: smooth and continuous

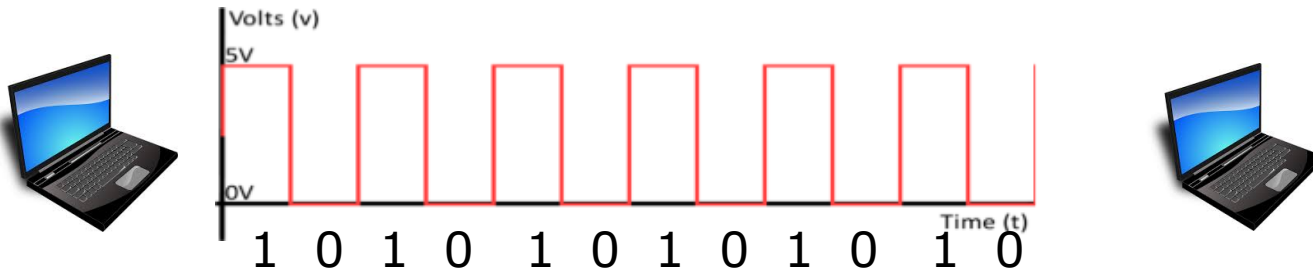


## Problems

1. Difficult to design
2. Susceptible to noise

Analog components: resistors, capacitors, inductors, diodes, e.t.c...

# ... to digital



Digital signals: discrete (encode sequence of 0s and 1s)

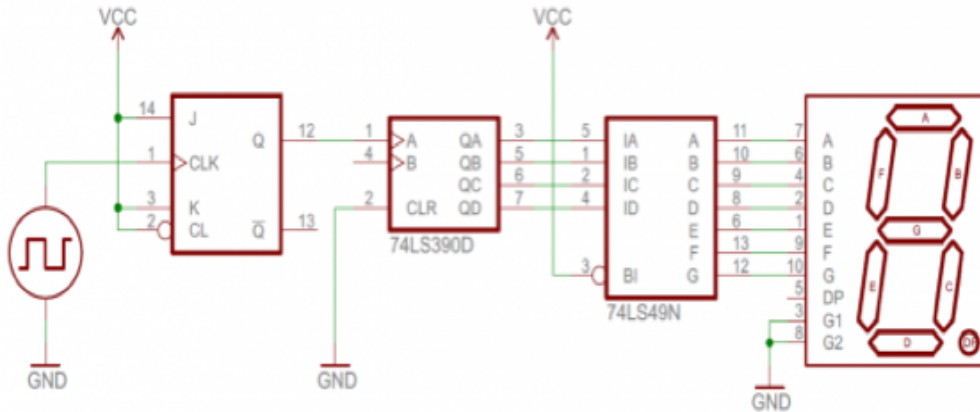
## Advantages

### 1. Easier to design

- Simple
- Integrate millions on a single chip

### 2. Reliable

- Robust to noise



Digital components: transistors, logic gates ...

# Using bits to represent everything

Bit = Binary digit, 0 or 1

A bit is too small to be used much

- A bit has two values; the English alphabet has 26 value (characters)

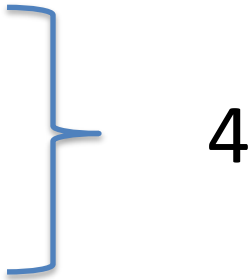
Using bits instead of bit

- Group bits together
- different possible bit patterns represent different “values”

# Question

- How many values can a group of 2 bits represent?

|   |   |
|---|---|
| 0 | 0 |
| 0 | 1 |
| 1 | 0 |
| 1 | 1 |



- How many values can a group of n bits represent?

$2^n$

Allow us to represent  
0, 1, 2, ... ( $2^n - 1$ )

# Represent non-negative integer

bits:  $b_{n-1}b_{n-2}\dots b_2b_1b_0$

**Question:** how to map each bit pattern to a unique integer in  $[0, 2^n - 1]$ ?

**Solution:** Base-2 representation

$$b_{n-1}b_{n-2}\dots b_2b_1b_0 = \sum_{i=0}^{n-1} b_i * 2^i$$

$b_i$  is bit at  $i$ -th position  
(from right to left,  
starting  $i=0$ )

# Most significant bit (MSB)

The bit position has the greatest value

Bits      01010

MSB      ?

Bits      11011010

MSB      ?

# Most significant bit (MSB)

The bit position has the greatest value  
– The leftmost bit

Bits      01010

MSB      0

Bits      11011010

MSB      1



# Least significant bit (LSB)

The bit position has the least value  
– The rightmost bit

Bits      01010

MSB      0

Bits      11011010

MSB      0

# Examples

Bits 0110

Value  $0*2^3 + 1*2^2 + 1*2^1 + 0*2^0 = 6$

Bits 1110

Value ?

$$1*2^3 + 1*2^2 + 1*2^1 + 0*2^0 = 14$$

# Byte

Each memory unit has multiple bits

- Dr. Werner Buchholz in July 1956
- Byte sizes from 1 bit to 48 bits have been used in the history

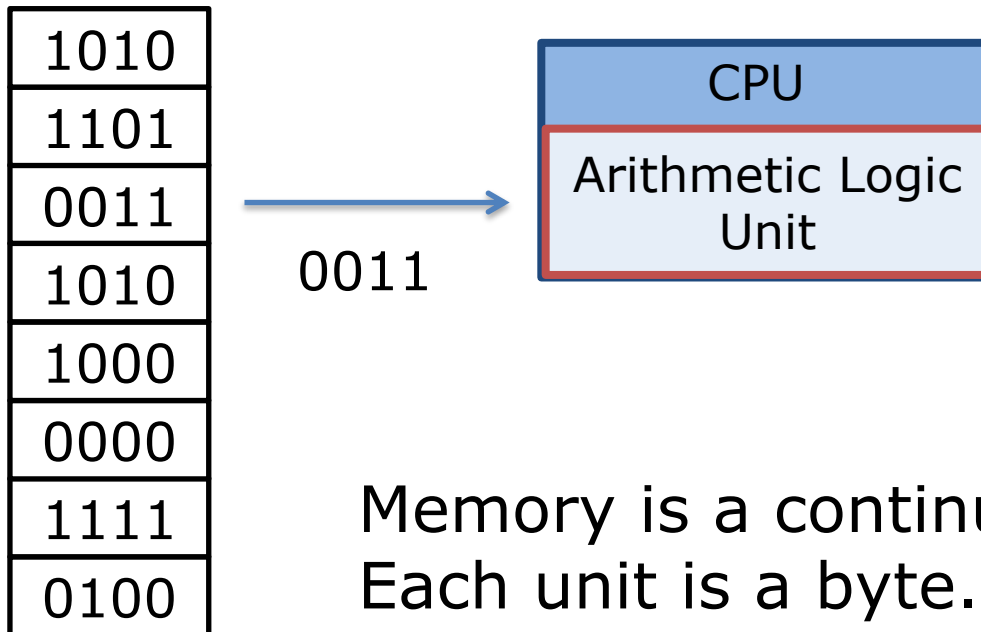


# Byte



Each memory unit has multiple bits

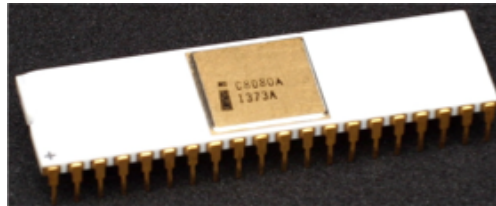
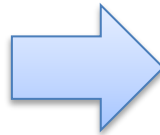
- Dr. Werner Buchholz in July 1956
- Byte sizes from 1 bit to 48 bits have been used in the history



Memory is a continuous array.  
Each unit is a byte.

Memory

# Byte – 8 bits chunk



IBM System/360, 1964

Intel 8080, 1974

Modern processors

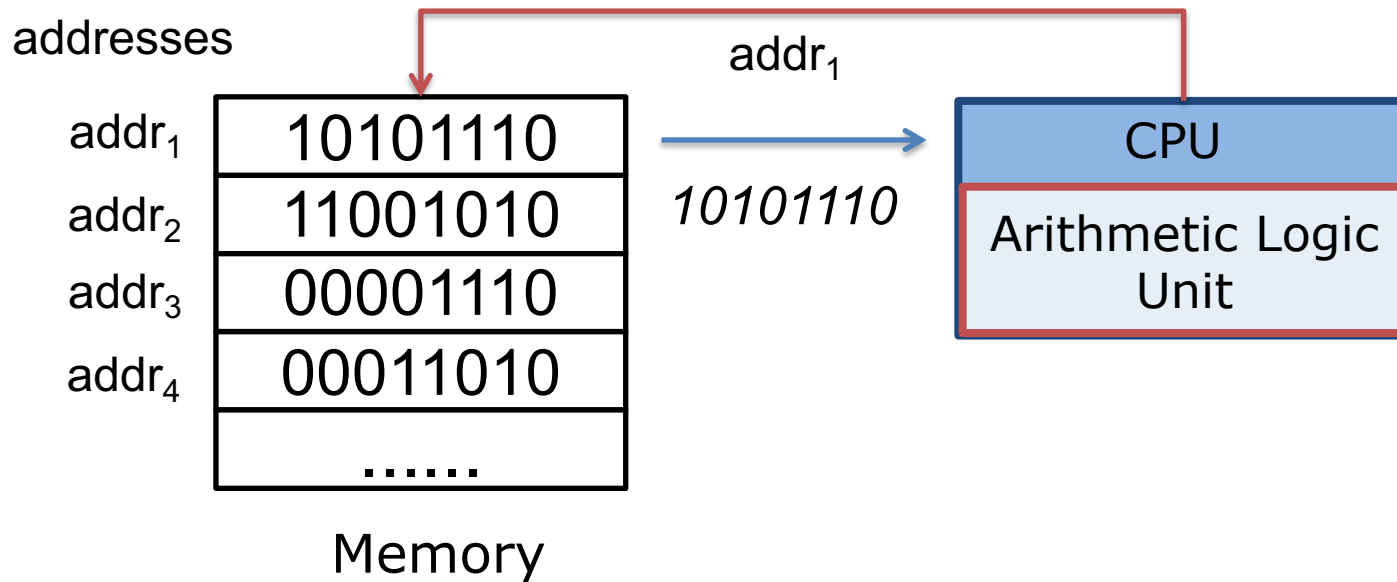
Introduce

Widely adopted

Standard

# Your mental model

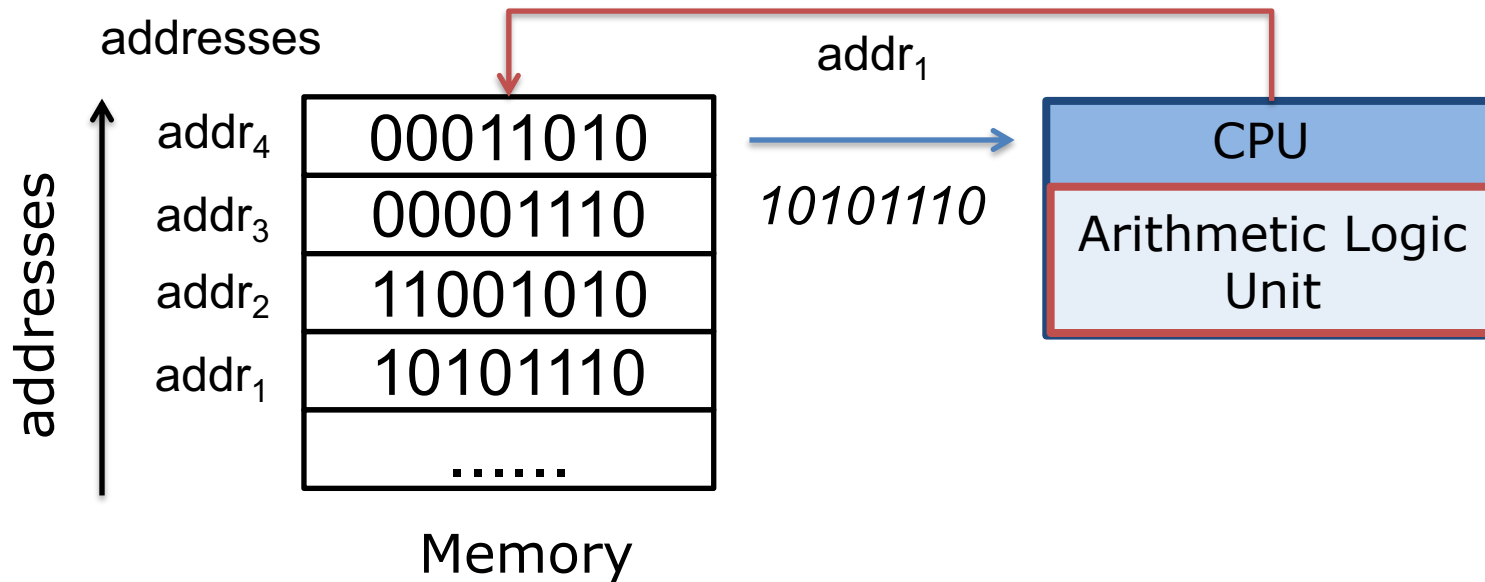
**Bits** 10101110 11001010 00001110 00011010



Each byte has 8 bits

# Your mental model

**Bits** 10101110 11001010 00001110 00011010



Each byte has 8 bits

# Range of Single Byte

Maximum

Minimum



# Range of Single Byte

Maximum

–  $11111111_2 \rightarrow 255$

Minimum

# Range of Single Byte

Maximum

$$- 11111111_2 \rightarrow 255$$


Minimum

$$- 00000000_2 \rightarrow 0$$

# Bit pattern description – intuitive way

Binary notation

Bits 10101110 11001010 00001110 00011010




4 bytes

# Bit pattern description – intuitive way

Binary notation

– Too verbose

Bits 10101110 11001010 00001110 00011010



4 bytes

15 cm on my laptop

# Bit pattern description – strawman

## Decimal Notation

– how many decimal digits to represent one byte? 3

|                |                 |                 |                 |                 |
|----------------|-----------------|-----------------|-----------------|-----------------|
| <b>Bits</b>    | <b>10101110</b> | <b>11001010</b> | <b>00001110</b> | <b>00011010</b> |
| <b>Decimal</b> | <b>174</b>      | <b>202</b>      | <b>014</b>      | <b>026</b>      |

# Bit pattern description – strawman

## Decimal Notation

– 3 decimal digits to represent one byte

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |

too tedious to do the conversion

# Hexadecimal Notation

Write bit patterns as base-16 (hex) numbers

- Hex “digit” is one of 16 symbols: 0-9, a,b,c,d,e,f
- Each byte is two 4-bit chunks
- Each 4-bit-chunk is represented by a hex “digit”

# Hexadecimal "digit"

| Hex | Decimal | Binary |
|-----|---------|--------|
| 0   | 0       | 0000   |
| 1   | 1       | 0001   |
| 2   | 2       | 0010   |
| 3   | 3       | 0011   |
| 4   | 4       | 0100   |
| 5   | 5       | 0101   |
| 6   | 6       | 0110   |
| 7   | 7       | 0111   |
| 8   | 8       | 1000   |
| 9   | 9       | 1001   |
| A   | 10      | 1010   |
| B   | 11      | 1011   |
| C   | 12      | 1100   |
| D   | 13      | 1101   |
| E   | 14      | 1110   |
| F   | 15      | 1111   |



# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     |          |          |          |          |
| Hex (C) |          |          |          |          |

1010 =

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |                  |          |          |          |
|---------|------------------|----------|----------|----------|
| Bits    | <b>1010</b> 1110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174              | 202      | 014      | 026      |
| Hex     | <b>A</b>         |          |          |          |
| Hex (C) |                  |          |          |          |

$$1010 = 1 * 2^3 + 0 * 2^2 + 1 * 2 + 0 = 10 = A_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |                  |          |          |          |
|---------|------------------|----------|----------|----------|
| Bits    | 1010 <b>1110</b> | 11001010 | 00001110 | 00011010 |
| Decimal | 174              | 202      | 014      | 026      |
| Hex     | A                |          |          |          |
| Hex (C) |                  |          |          |          |

1110 =

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |                  |          |          |          |
|---------|------------------|----------|----------|----------|
| Bits    | 1010 <b>1110</b> | 11001010 | 00001110 | 00011010 |
| Decimal | 174              | 202      | 014      | 026      |
| Hex     | A <b>E</b>       |          |          |          |
| Hex (C) |                  |          |          |          |

$$1110 = 1 * 2^3 + 1 * 2^2 + 1 * 2 + 0 = 14 = E_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A        | E        |          |          |
| Hex (C) |          |          |          |          |

1100 =

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |      |      |          |          |
|---------|----------|------|------|----------|----------|
| Bits    | 10101110 | 1100 | 1010 | 00001110 | 00011010 |
| Decimal | 174      | 202  |      | 014      | 026      |
| Hex     | A        | E    | C    |          |          |
| Hex (C) |          |      |      |          |          |

$$1100 = 1 * 2^3 + 1 * 2^2 + 0 * 2 + 0 = 12 = C_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A E      | C        |          |          |
| Hex (C) |          |          |          |          |

1010 =

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A E      | C A      |          |          |
| Hex (C) |          |          |          |          |

$$1010 = 1 * 2^3 + 0 * 2^2 + 1 * 2 + 0 = 10 = A_{16}$$



# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A E      | C A      | 0        |          |
| Hex (C) |          |          |          |          |

$$0000 = 0 * 2^3 + 0 * 2^2 + 0 * 2 + 0 = 0 = 0_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A E      | C A      | 0 E      |          |
| Hex (C) |          |          |          |          |

$$1110 = 1 * 2^3 + 1 * 2^2 + 1 * 2 + 0 = 14 = E_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A E      | C A      | 0 E      | 1        |
| Hex (C) |          |          |          |          |

$$0001 = 0 * 2^3 + 0 * 2^2 + 0 * 2 + 1 = 1 = 1_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |          |          |          |          |
|---------|----------|----------|----------|----------|
| Bits    | 10101110 | 11001010 | 00001110 | 00011010 |
| Decimal | 174      | 202      | 014      | 026      |
| Hex     | A E      | C A      | 0 E      | 1 A      |
| Hex (C) |          |          |          |          |

$$1010 = 1 * 2^3 + 0 * 2^2 + 1 * 2 + 0 = 10 = A_{16}$$

# Hexadecimal Notation

- Each byte is represented with 2 hex numbers ( $00_{16}$  --  $FF_{16}$ )

|         |            |          |          |          |
|---------|------------|----------|----------|----------|
| Bits    | 10101110   | 11001010 | 00001110 | 00011010 |
| Decimal | 174        | 202      | 014      | 026      |
| Hex     | A E        | C A      | 0 E      | 1 A      |
| Hex (C) | 0xAECA0E1A |          |          |          |

# Exercises Time

Hexadecimal

Decimal

Binary

1010 0111

0011 1110

0xBC

55

0xF3

# Answers

| Hexadecimal | Decimal              | Binary    |
|-------------|----------------------|-----------|
| 0xA7        | $10 * 16 + 7 = 167$  | 1010 0111 |
| 0x3E        | $3 * 16 + 14 = 62$   | 0011 1110 |
| 0xBC        | $11 * 16 + 12 = 188$ | 1011 1100 |
| 0x37        | $3 * 16 + 7 = 55$    | 0011 0111 |
| 0xF3        | $15 * 16 + 3 = 243$  | 1111 0011 |

# Unsigned addition



11 + 10



0xB + 0xA



00001011<sub>2</sub> + 00001010<sub>2</sub>



# Unsigned addition



11 + 10



0xB + 0xA



00001011<sub>2</sub> + 00001010<sub>2</sub>

```
    0 0 0 0 1 0 1 1
+   0 0 0 0 1 0 1 0
-----
```

# Unsigned addition



11 + 10



0xB + 0xA



00001011<sub>2</sub> + 00001010<sub>2</sub>

0 0 0 0 1 0 1 1  
+ 0 0 0 0 1 0 1 0

---

1

# Unsigned addition



11 + 10



0xB + 0xA



$00001011_2 + 00001010_2$

0 0 0 0 1 0 1 1  
+ 0 0 0 0 1 0 1 0

---

2 1

# Unsigned addition



11 + 10

0xB + 0xA

00001011<sub>2</sub> + 00001010<sub>2</sub>

$$\begin{array}{r} \phantom{+} 000010\mathbf{1}1 \\ + 000010\mathbf{1}0 \\ \hline \phantom{+} 00010\mathbf{0}1 \end{array}$$

# Unsigned addition



11 + 10

0xB + 0xA

00001011<sub>2</sub> + 00001010<sub>2</sub>

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
|   |   |   |   |   |   | 1 |   |   |
|   | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 |
| + | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
|   |   |   |   |   |   |   |   |   |
|   |   |   |   |   | 1 | 0 | 1 |   |

# Unsigned addition



11 + 10



0xB + 0xA



00001011<sub>2</sub> + 00001010<sub>2</sub>

```
      0 0 0 0 1 0 1 1
+     0 0 0 0 1 0 1 0
-----
      0 0 0 1 0 1 0 1
```

# Unsigned subtraction



11 - 10



0xB - 0xA



00001011<sub>2</sub> - 00001010<sub>2</sub>

```
      0 0 0 0 1 0 1 1
-     0 0 0 0 1 0 1 0
-----
      0 0 0 0 0 0 0 1
```

# Unsigned subtraction



11 - 10



0xB - 0xA



00001011<sub>2</sub> - 00001010<sub>2</sub>

$$\begin{array}{r} 00001011 \\ - 00001010 \\ \hline 00000001 \end{array}$$



# Unsigned subtraction



10 - 11

0xA - 0xB

00001010<sub>2</sub> - 00001011<sub>2</sub>

```
  0 0 0 0 1 0 1 0
-  0 0 0 0 1 0 1 1
-----
```

???

**Question:**

How to represent negative numbers?

# Strawman

Most significant bit (MSB) represent the sign

$$0\ 0\ 0\ 0\ 0\ 0\ 0\ 1_2 \rightarrow 1$$

$$1\ 0\ 0\ 0\ 0\ 0\ 0\ 1_2 \rightarrow -1$$

$$\begin{array}{r} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1 \\ +\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1 \\ \hline \end{array}$$

# Strawman

Most significant bit (MSB) represent the sign

$$0\ 0\ 0\ 0\ 0\ 0\ 0\ 1_2 \rightarrow 1$$

$$1\ 0\ 0\ 0\ 0\ 0\ 0\ 1_2 \rightarrow -1$$

$$\begin{array}{r} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1 \\ +\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1 \\ \hline 1\ 0\ 0\ 0\ 0\ 0\ 1\ 0 \end{array}$$

# Strawman

Most significant bit (MSB) represent the sign

$$0\ 0\ 0\ 0\ 0\ 0\ 0\ 1_2 \rightarrow 1$$

$$1\ 0\ 0\ 0\ 0\ 0\ 0\ 1_2 \rightarrow -1$$

$$\begin{array}{r} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1 \\ +\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1 \\ \hline 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0 \end{array}$$

-2 ???



# Two's complement

Byte 10010110

Unsigned number

$$1 * 2^7 + 0 * 2^6 + 0 * 2^5 + 1 * 2^4 + 0 * 2^3 + 1 * 2^2 + 1 * 2 + 0 * 2^0$$

# Two's complement

Byte 10010110

Unsigned number

$$1 * 2^7 + 0 * 2^6 + 0 * 2^5 + 1 * 2^4 + 0 * 2^3 + 1 * 2^2 + 1 * 2 + 0 * 2^0$$

Signed number

$$-1 * 2^7 + 0 * 2^6 + 0 * 2^5 + 1 * 2^4 + 0 * 2^3 + 1 * 2^2 + 1 * 2 + 0 * 2^0$$

# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0] \quad \text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

$$\text{MSB: } \text{val}(b_w) = -b_w * 2^w$$

$$\text{Other: } \text{val}(b_i) = b_i * 2^i, \quad 0 \leq i < w$$



# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0]$$

$$\text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

Binary

1000 0001

1010 0101

0101 0101

Value

# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0]$$

$$\text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

Binary

1000 0001

1010 0101

0101 0101

$$-1 * 2^7 + 1$$

Value

-127

# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0] \quad \text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

| Binary    |                              | Value |
|-----------|------------------------------|-------|
| 1000 0001 | $-1 * 2^7 + 1$               | -127  |
| 1010 0101 | $-1 * 2^7 + 2^5 + 2^2 + 2^0$ | -91   |
| 0101 0101 |                              |       |

# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0] \quad \text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

| Binary    |                              | Value |
|-----------|------------------------------|-------|
| 1000 0001 | $-1 * 2^7 + 1$               | -127  |
| 1010 0101 | $-1 * 2^7 + 2^5 + 2^2 + 2^0$ | -91   |
| 0101 0101 | $2^6 + 2^4 + 2^2 + 2$        | 85    |

# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0]$$

$$\text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

0 0 0 0 0 0 0 1

+ 1 0 0 0 0 0 0 1

---

1 0 0 0 0 0 1 0

# Two's complement

$$\vec{b} = [b_w, b_{w-1}, \dots, b_0]$$

$$\text{val}(\vec{b}) = -b_w 2^w + \sum_{i=0}^{w-1} b_i 2^i$$

0 0 0 0 0 0 0 1

$2^0$

1

+ 1 0 0 0 0 0 0 1

$-1 * 2^7 + 2^0$

-127

---

1 0 0 0 0 0 1 0

$-1 * 2^7 + 2^1$

-126

# Find 2's complement quickly

With a negative number, how to give its binary representation? e.g. -40

# Find 2's complement quickly

With a negative number, how to give its binary representation? e.g. -40

Step 1. represent 40 in binary

0010 1000



# Find 2's complement quickly

With a negative number, how to give its binary representation? e.g. -40

Step 2. flip all bits

0010 1000 → 1101 0111

# Find 2's complement quickly

With a negative number, how to give its binary representation? e.g. -40

Step 3. add 1

0010 1000  $\rightarrow$  1101 0111  $\rightarrow$  1101 1000

# Find 2's complement quickly

With a negative number, how to give its binary representation? e.g. -40

Step 3. add 1

0010 1000 → 1101 0111 → 1101 1000

$$\begin{array}{r} 0010\ 1000 \\ +\ 1101\ 0111 \\ \hline 1111\ 1111 \end{array}$$

# Find 2's complement quickly

With a negative number, how to give its binary representation? e.g. -40

Step 3. add 1

0010 1000 → 1101 0111 → 1101 1000

$$\begin{array}{r} 0010\ 1000 \\ 1101\ 0111 \\ + \qquad \qquad 1 \\ \hline 1\ 0000\ 0000 \end{array}$$

# Why does this trick work

- What is  $1111\dots11_2$  in 2's complement?

- $\vec{b} + (\sim \vec{b}) = 11\dots11_2 = -1$

b with bits  
flipped

$$-\vec{b} = (\sim \vec{b}) + 1$$

# Exercise Time II

Hexadecimal

Decimal

Binary

0xce

1001 1100

127

-128

-90

# Answers

| Hexadecimal | Decimal | Binary    |
|-------------|---------|-----------|
| 0xce        | -50     | 1100 1110 |
| 0x9c        | -100    | 1001 1100 |
| 0x7f        | 127     | 0111 1111 |
| 0x80        | -128    | 1000 0000 |
| 0xa6        | -90     | 1010 0110 |

# Ranges

|                 | Range          | Min | Max |
|-----------------|----------------|-----|-----|
| 1 byte unsigned | $[0, 2^8 - 1]$ | 0   | 255 |
| 1 byte signed   |                |     |     |



# Ranges

|                 | Range             | Min  | Max |
|-----------------|-------------------|------|-----|
| 1 byte unsigned | $[0, 2^8 - 1]$    | 0    | 255 |
| 1 byte signed   | $[-2^7, 2^7 - 1]$ | -128 | 127 |

Min: 1000 0000

Max: 0111 1111

# Overflow

$$\begin{array}{r} 10000001 \\ + 10000001 \\ \hline \end{array}$$

|                 | Range             | Min  | Max |
|-----------------|-------------------|------|-----|
| 1 byte unsigned | $[0, 2^8 - 1]$    | 0    | 255 |
| 1 byte signed   | $[-2^7, 2^7 - 1]$ | -128 | 127 |

# Overflow

1 0 0 0 0 0 0 1      -127  
+ 1 0 0 0 0 0 0 1      -127

---

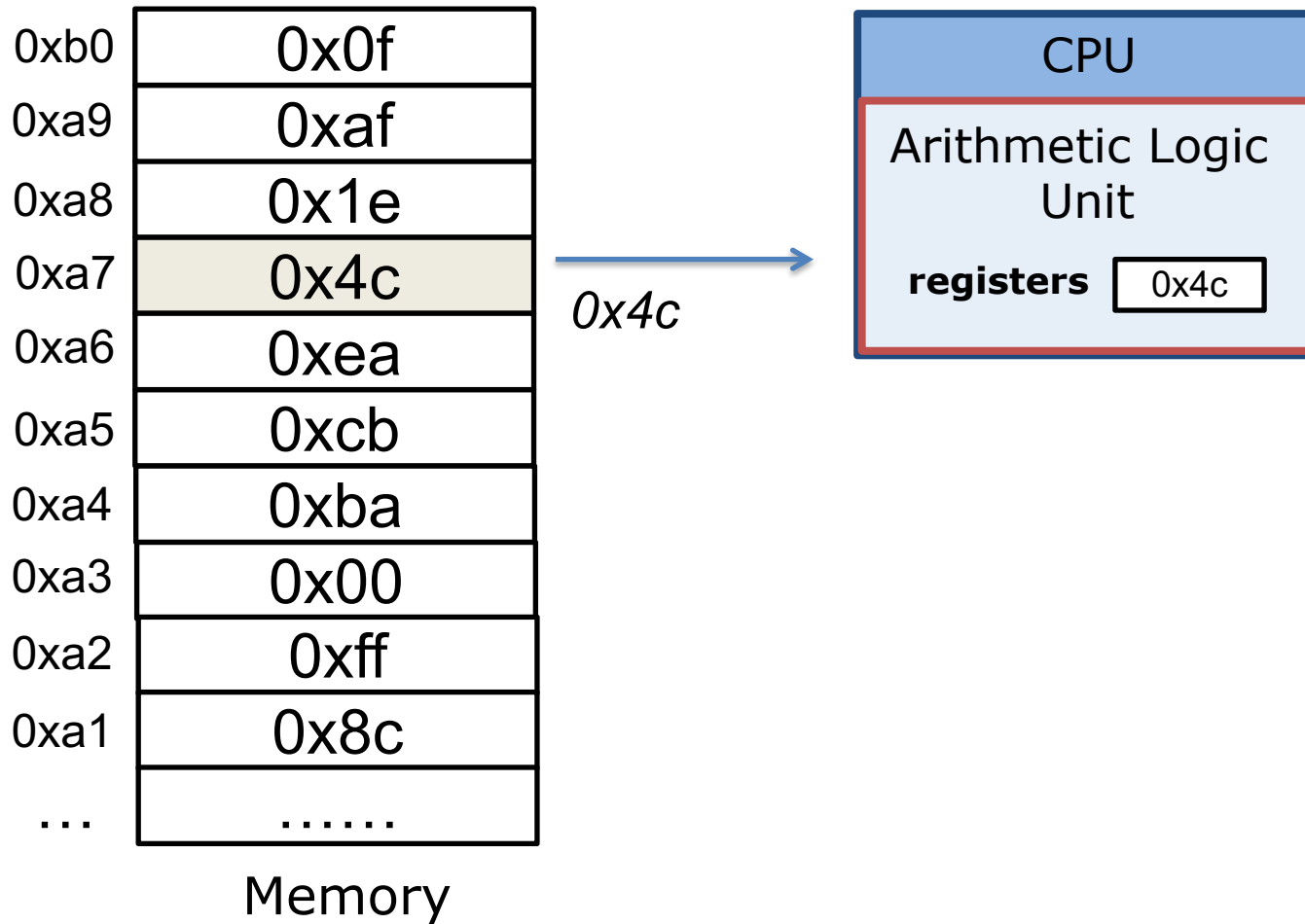
**1** 0 0 0 0 0 0 1 0

2 ???

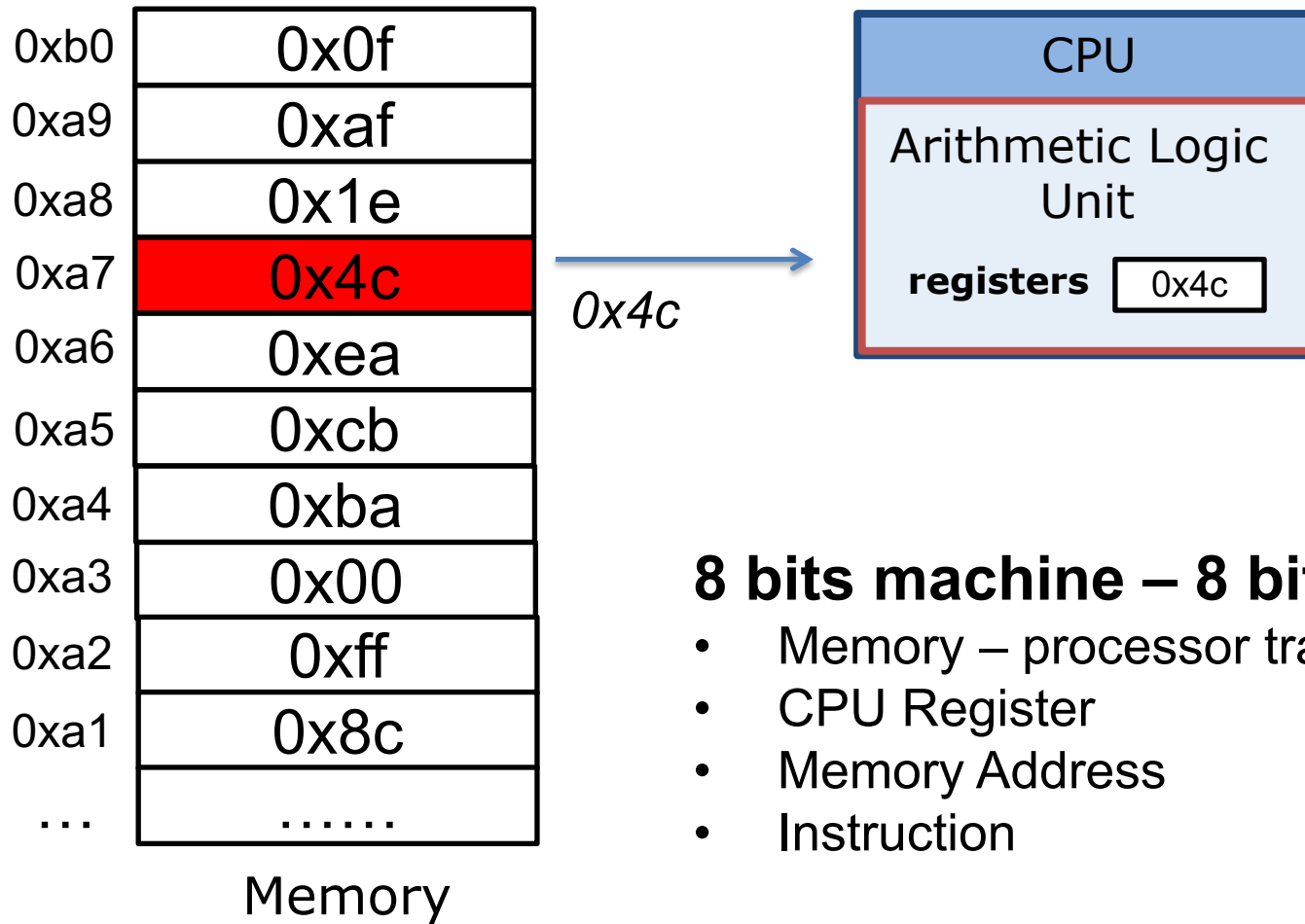


|                 | Range             | Min  | Max |
|-----------------|-------------------|------|-----|
| 1 byte unsigned | $[0, 2^8 - 1]$    | 0    | 255 |
| 1 byte signed   | $[-2^7, 2^7 - 1]$ | -128 | 127 |

# Intel 8080



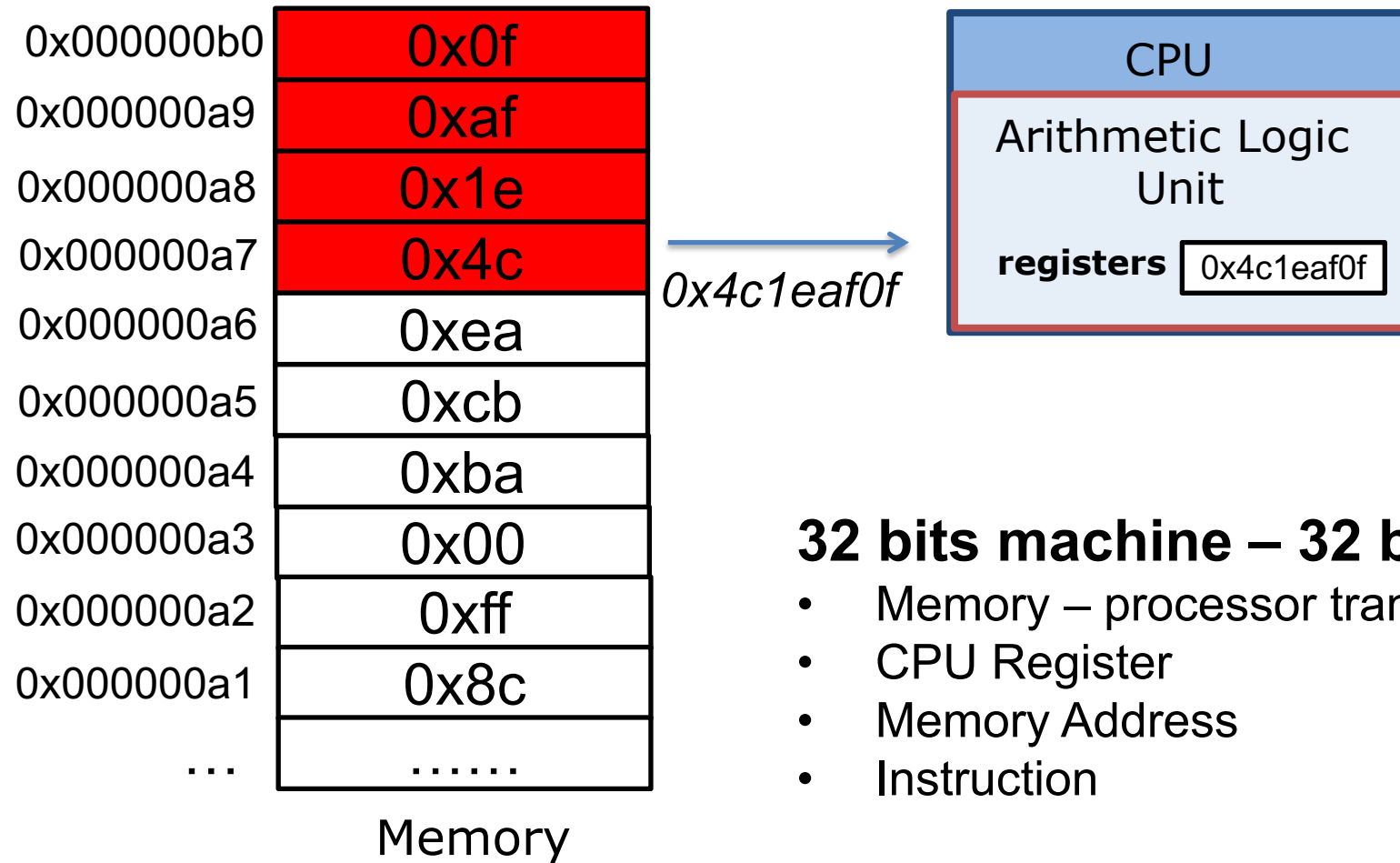
# Intel 8080



## 8 bits machine – 8 bits length of

- Memory – processor transfer
- CPU Register
- Memory Address
- Instruction

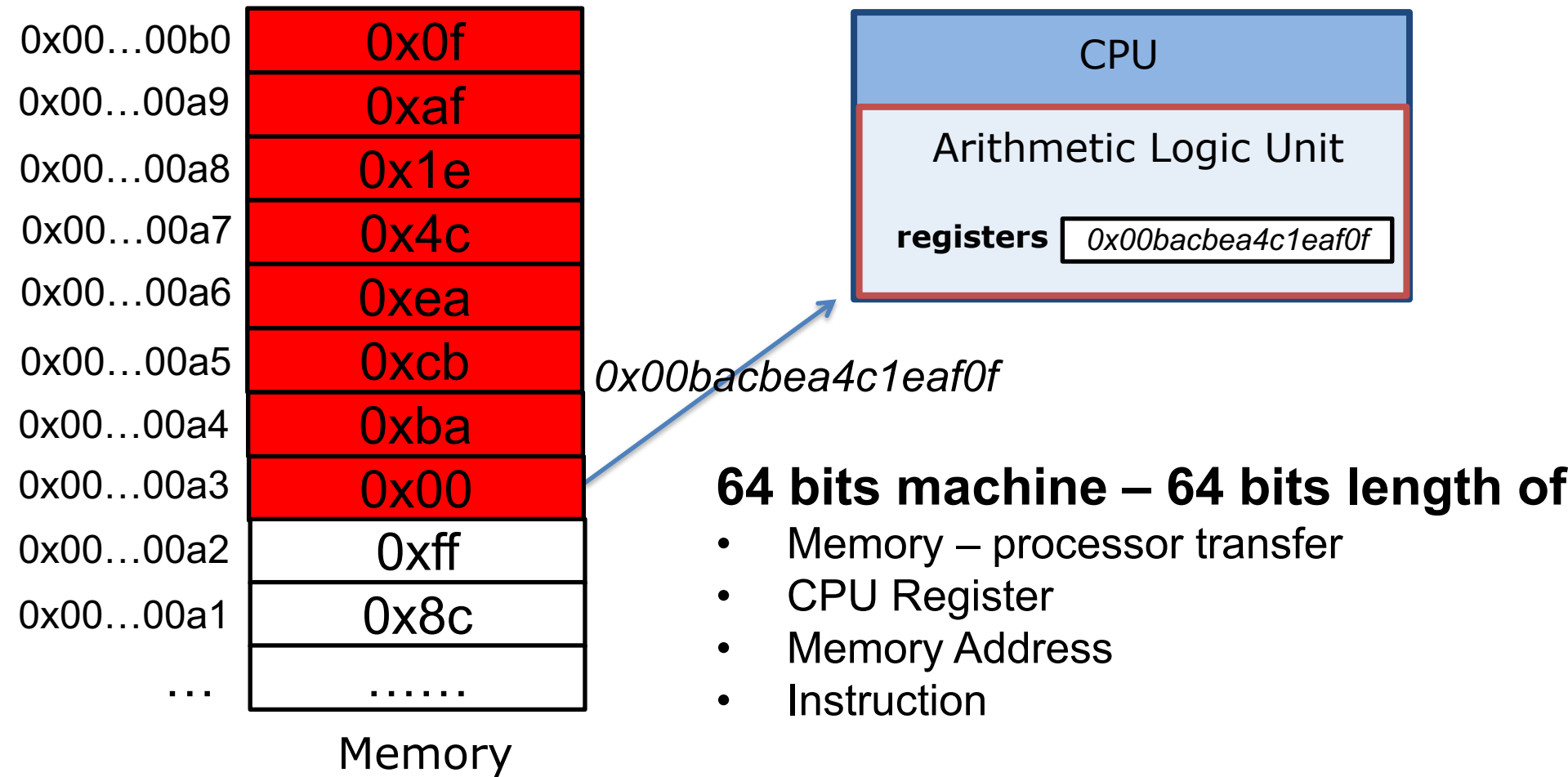
# Intel 386



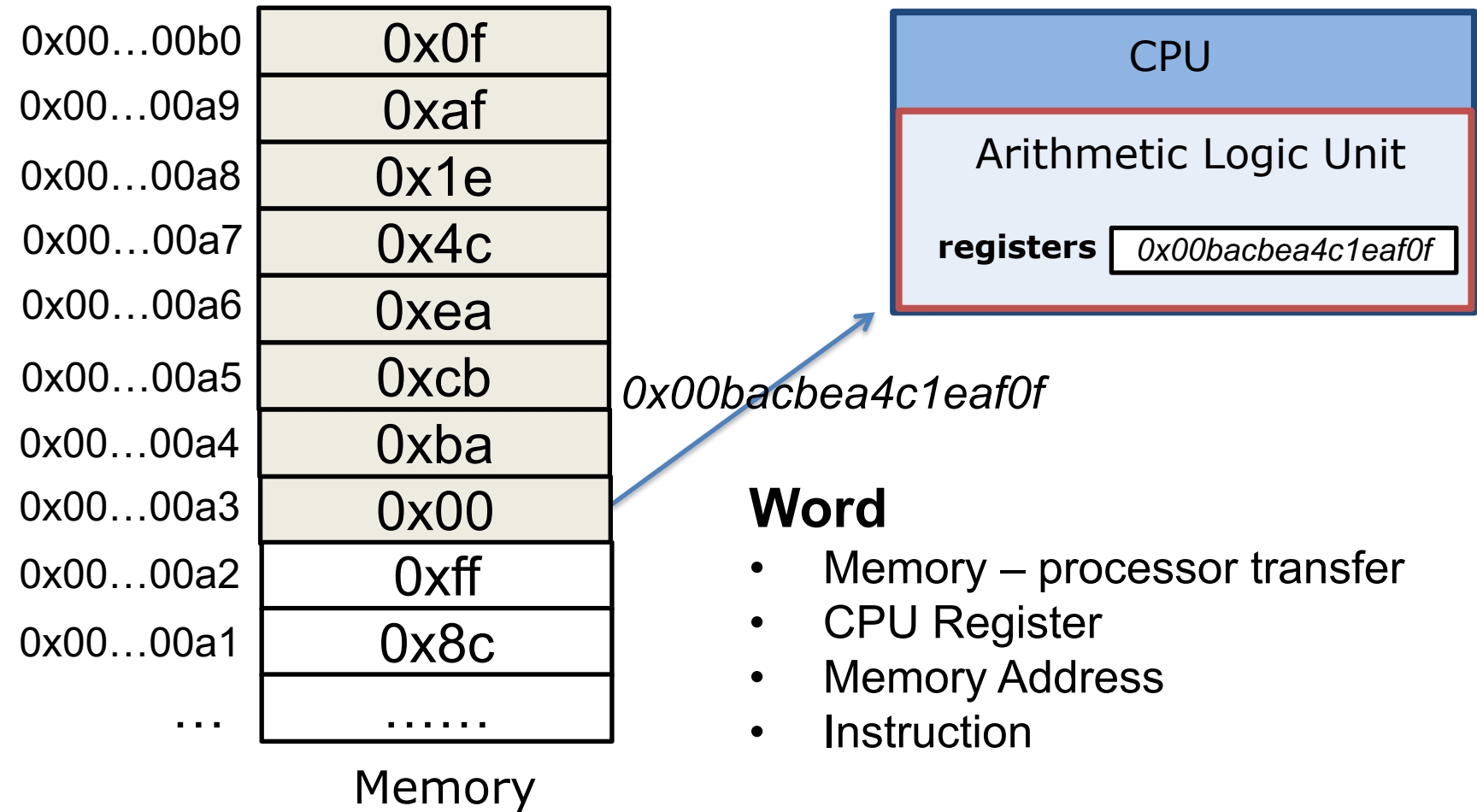
## 32 bits machine – 32 bits length of

- Memory – processor transfer
- CPU Register
- Memory Address
- Instruction

# Intel Opteron → i7



# Intel Opteron → i7





# Word

## Definition

- Fixed size of data handled as a unit by the instruction set or processor

## Length

- 8 for 8 bits machine
- 32 for 32 bits machine
- 64 for 64 bits machine

# C's integral data types on 64 bits machine

|                | Length  | Min    | Max       |
|----------------|---------|--------|-----------|
| [signed] char  | 1 byte  | $-2^7$ | $2^7 - 1$ |
| unsigned char  | 1 byte  | 0      | $2^8 - 1$ |
| short          | 2 bytes |        |           |
| unsigned short | 2 bytes |        |           |
| int            | 4 bytes |        |           |
| unsigned int   | 4 bytes |        |           |
| long           | 8 bytes |        |           |
| unsigned long  | 8 bytes |        |           |

# Integral data types on 64 bits machine

|                | Length  | Min       | Max          |
|----------------|---------|-----------|--------------|
| [signed] char  | 1 byte  | $-2^7$    | $2^7 - 1$    |
| unsigned char  | 1 byte  | 0         | $2^8 - 1$    |
| short          | 2 bytes | $-2^{15}$ | $2^{15} - 1$ |
| unsigned short | 2 bytes | 0         | $2^{16} - 1$ |
| int            | 4 bytes |           |              |
| unsigned int   | 4 bytes |           |              |
| long           | 8 bytes |           |              |
| unsigned long  | 8 bytes |           |              |

# Integral data types on 64 bits machine

|                | Length  | Min       | Max          |
|----------------|---------|-----------|--------------|
| [signed] char  | 1 byte  | $-2^7$    | $2^7 - 1$    |
| unsigned char  | 1 byte  | 0         | $2^8 - 1$    |
| short          | 2 bytes | $-2^{15}$ | $2^{15} - 1$ |
| unsigned short | 2 bytes | 0         | $2^{16} - 1$ |
| int            | 4 bytes | $-2^{31}$ | $2^{31} - 1$ |
| unsigned int   | 4 bytes | 0         | $2^{32} - 1$ |
| long           | 8 bytes |           |              |
| unsigned long  | 8 bytes |           |              |

# Integral data types on 64 bits machine

|                | Length  | Min       | Max          |
|----------------|---------|-----------|--------------|
| [signed] char  | 1 byte  | $-2^7$    | $2^7 - 1$    |
| unsigned char  | 1 byte  | 0         | $2^8 - 1$    |
| short          | 2 bytes | $-2^{15}$ | $2^{15} - 1$ |
| unsigned short | 2 bytes | 0         | $2^{16} - 1$ |
| int            | 4 bytes | $-2^{31}$ | $2^{31} - 1$ |
| unsigned int   | 4 bytes | 0         | $2^{32} - 1$ |
| long           | 8 bytes | $-2^{63}$ | $2^{63} - 1$ |
| unsigned long  | 8 bytes | 0         | $2^{64} - 1$ |

# Your first C program

```
#include <stdio.h>

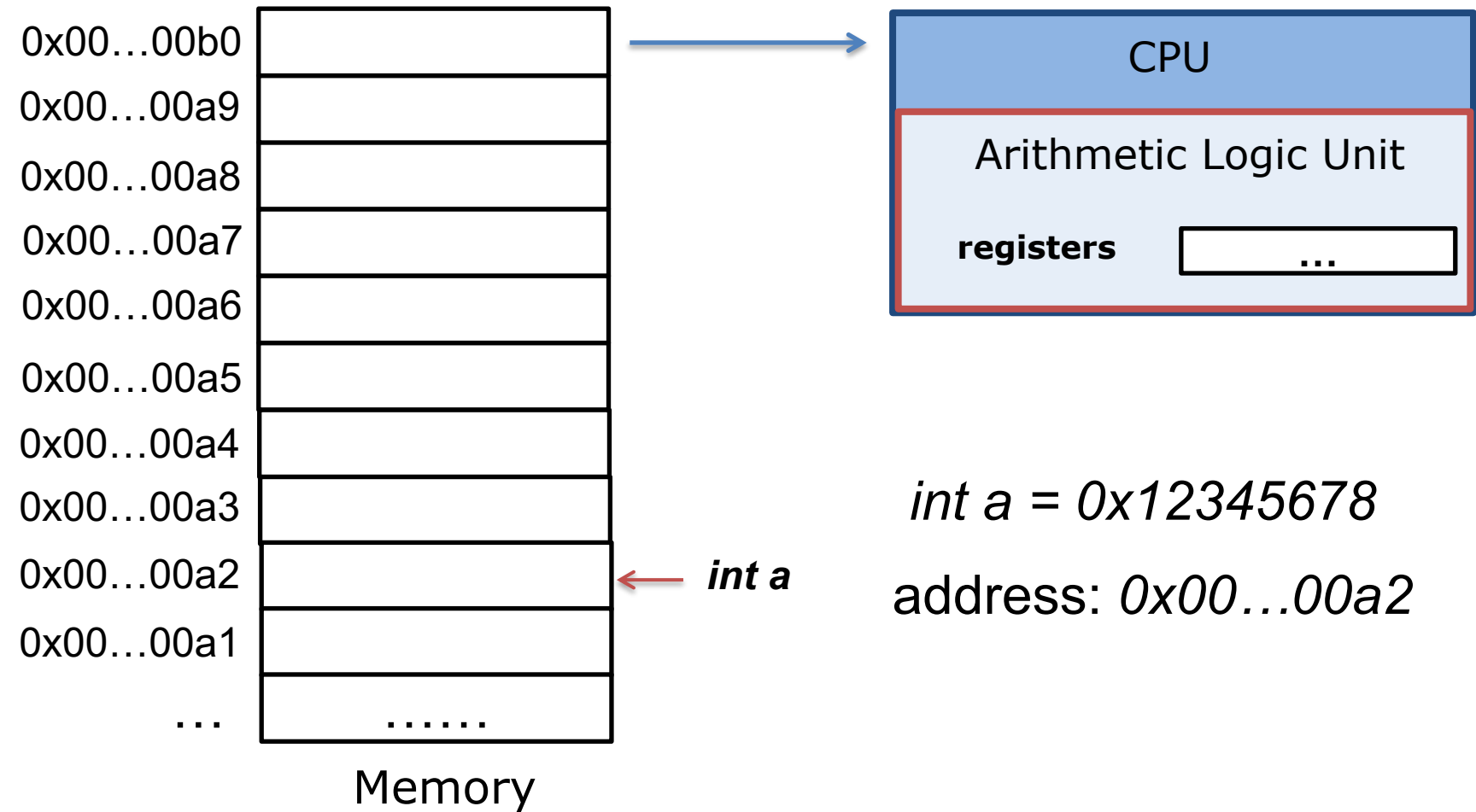
int
main()
{
    char x = -127;
    char y = 0x81;
    char z = x + y;
    printf("hello world sum is %d\n", z);
}
```

```
$ gcc helloworld.c
```

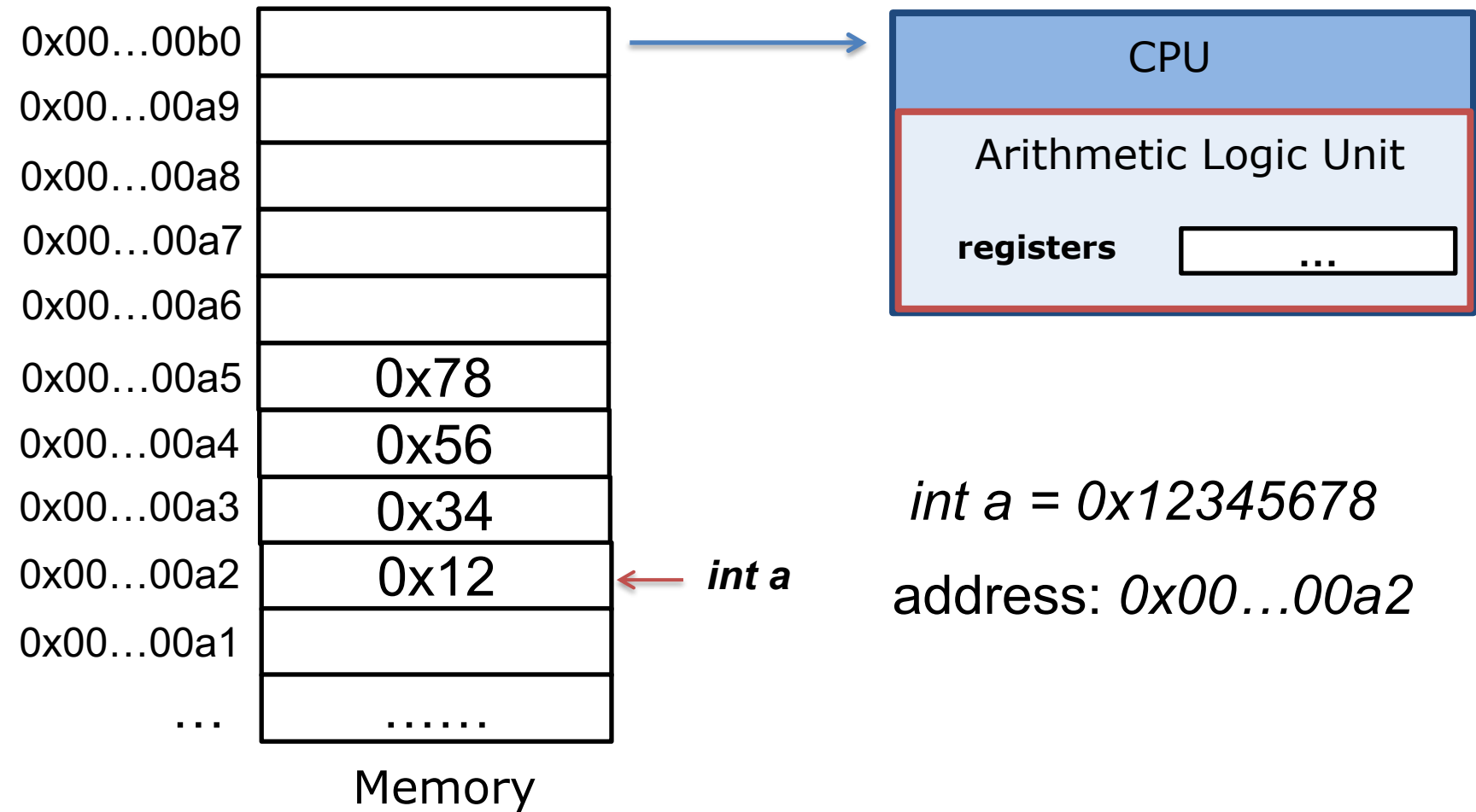
```
$ ./a.out
```

|   |          |   |   |   |   |   |   |   |      |   |
|---|----------|---|---|---|---|---|---|---|------|---|
|   | 1        | 0 | 0 | 0 | 0 | 0 | 0 | 1 | -127 |   |
| + | 1        | 0 | 0 | 0 | 0 | 0 | 0 | 1 | -127 |   |
|   | <b>1</b> | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0    | 2 |

# Memory layout

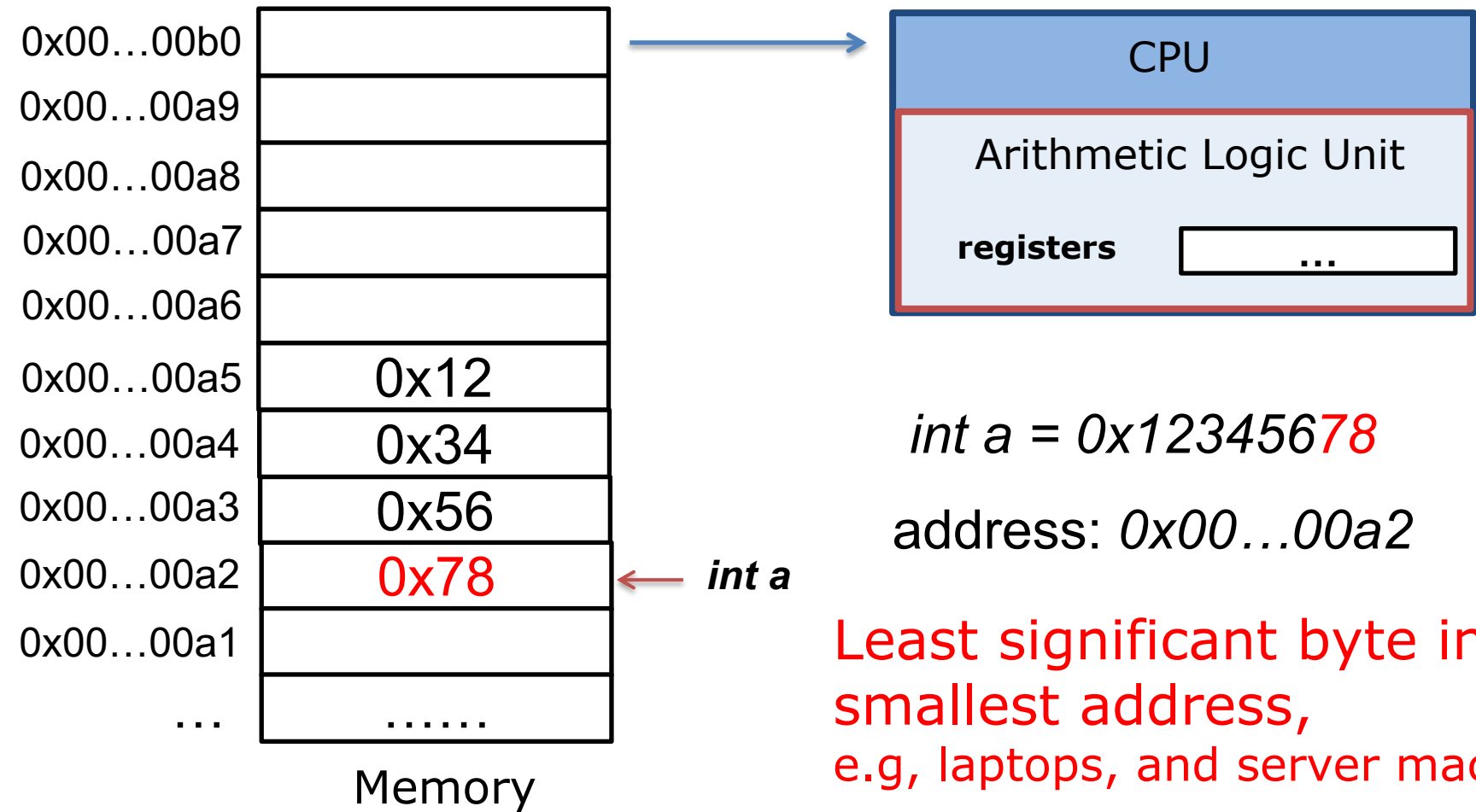


# Memory layout – Intuition






# Memory layout – Little Endian



# Advantages of Little Endian

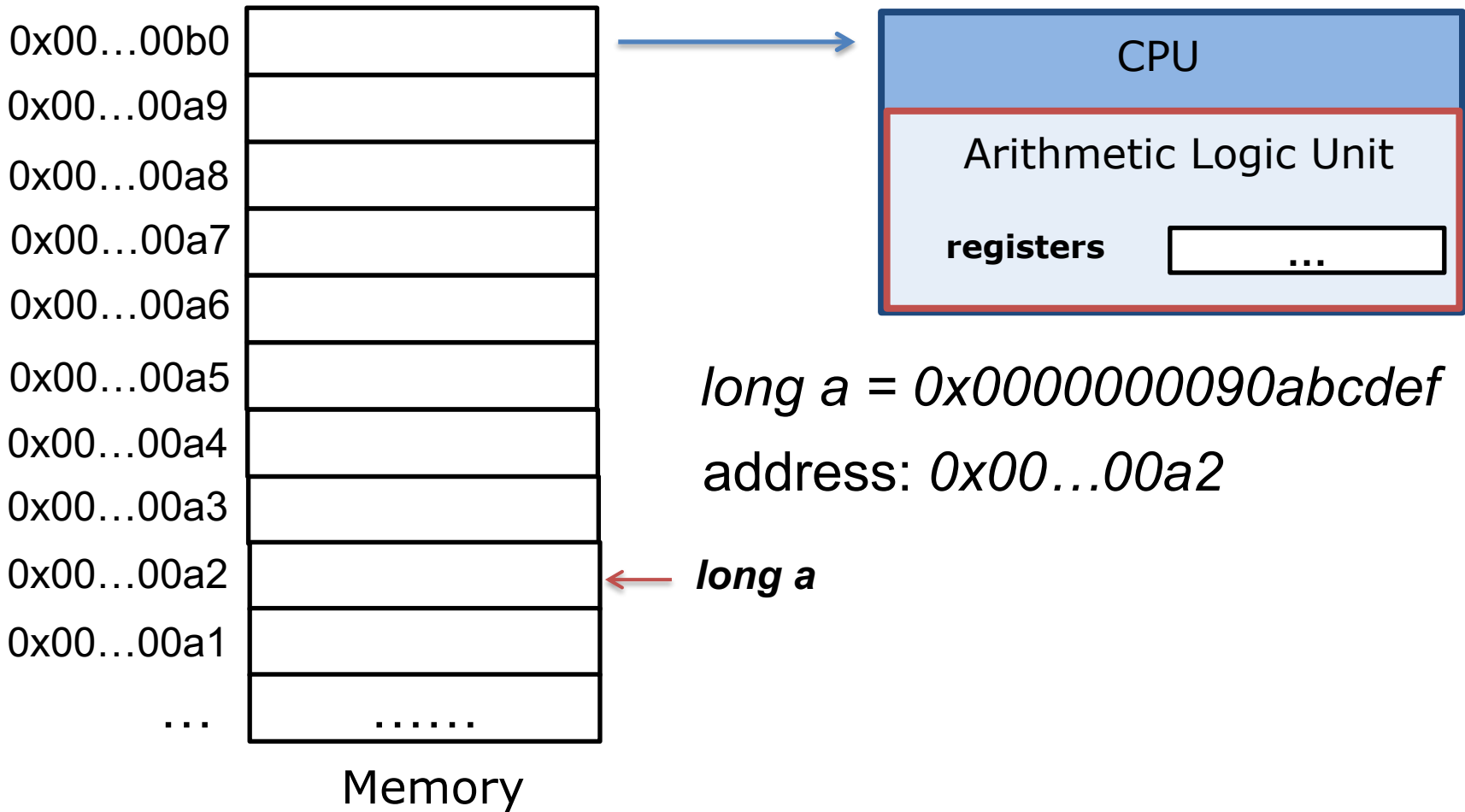
0x12345678  
+ 0x12131415  


Processor performs the calculation from the least significant bit

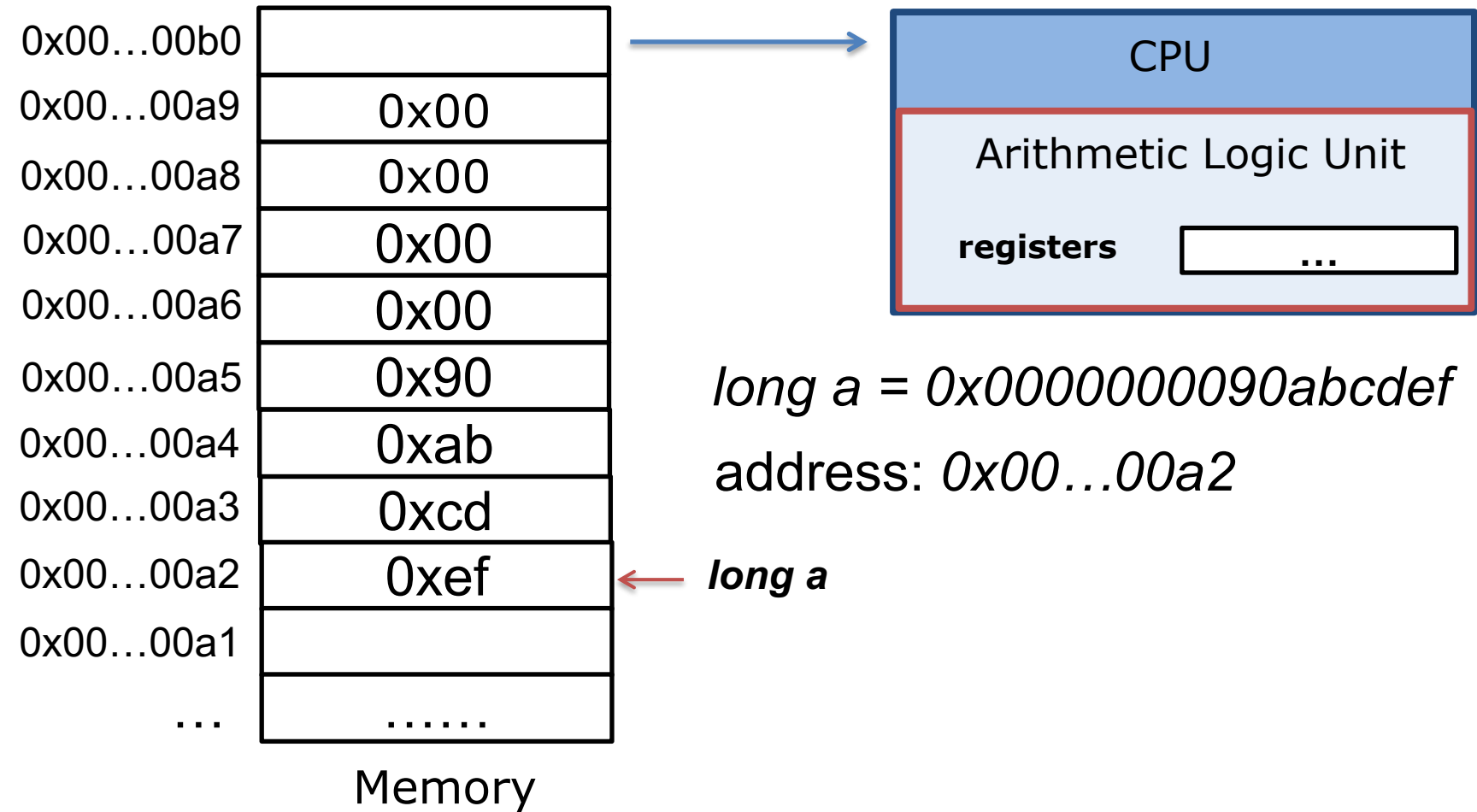


Processor can simultaneously perform memory transfer and calculation.

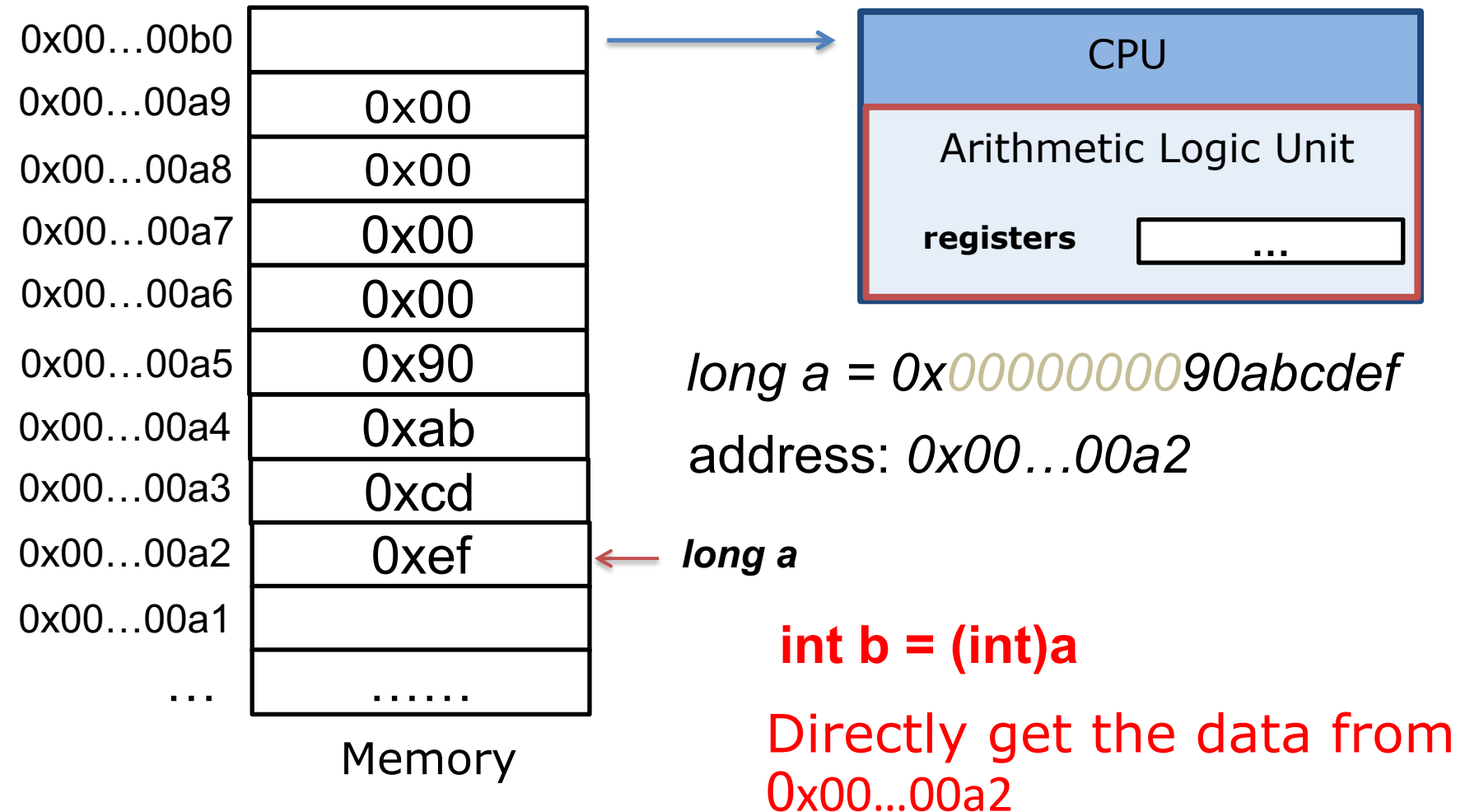
# Advantages of Little Endian



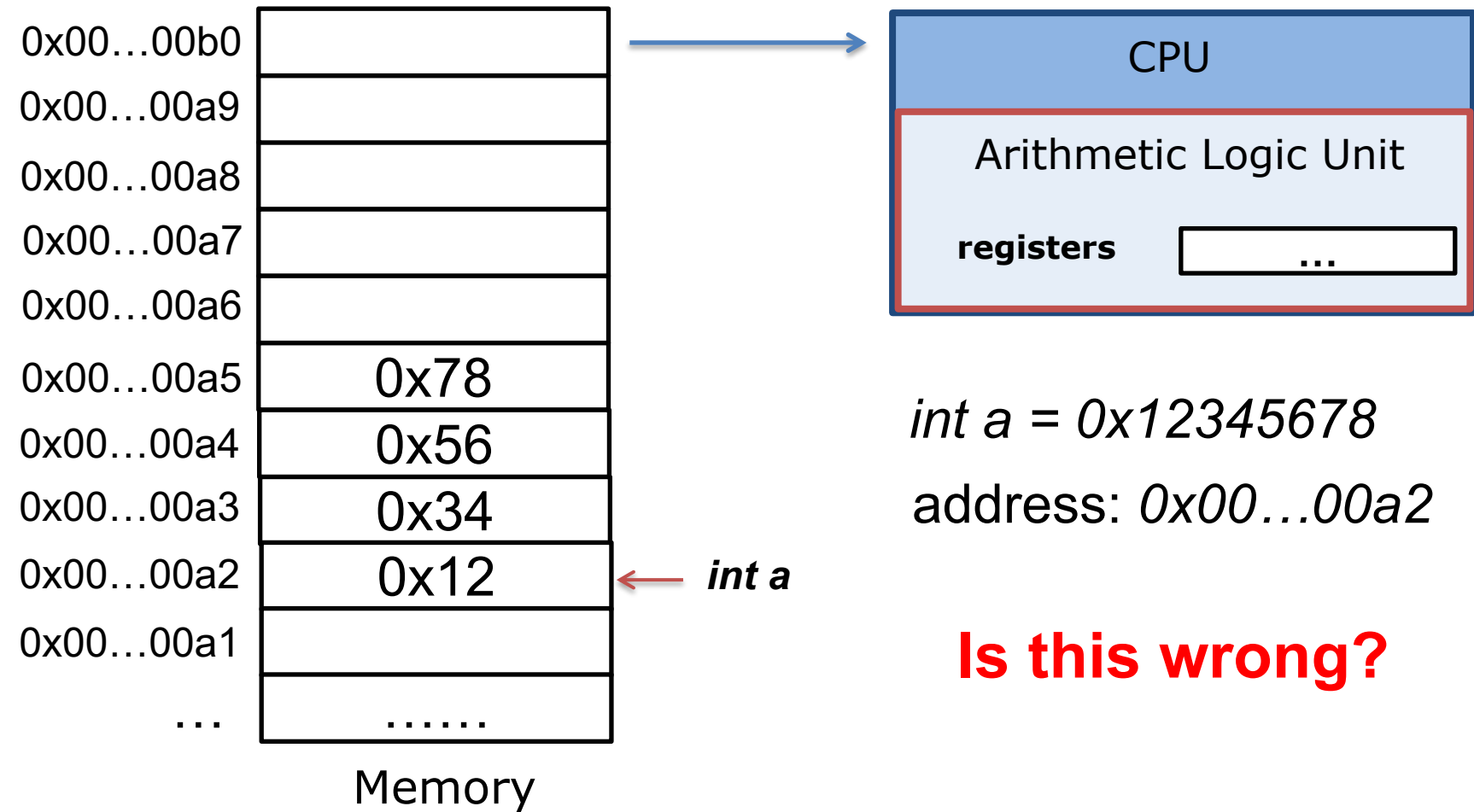
# Advantages of Little Endian



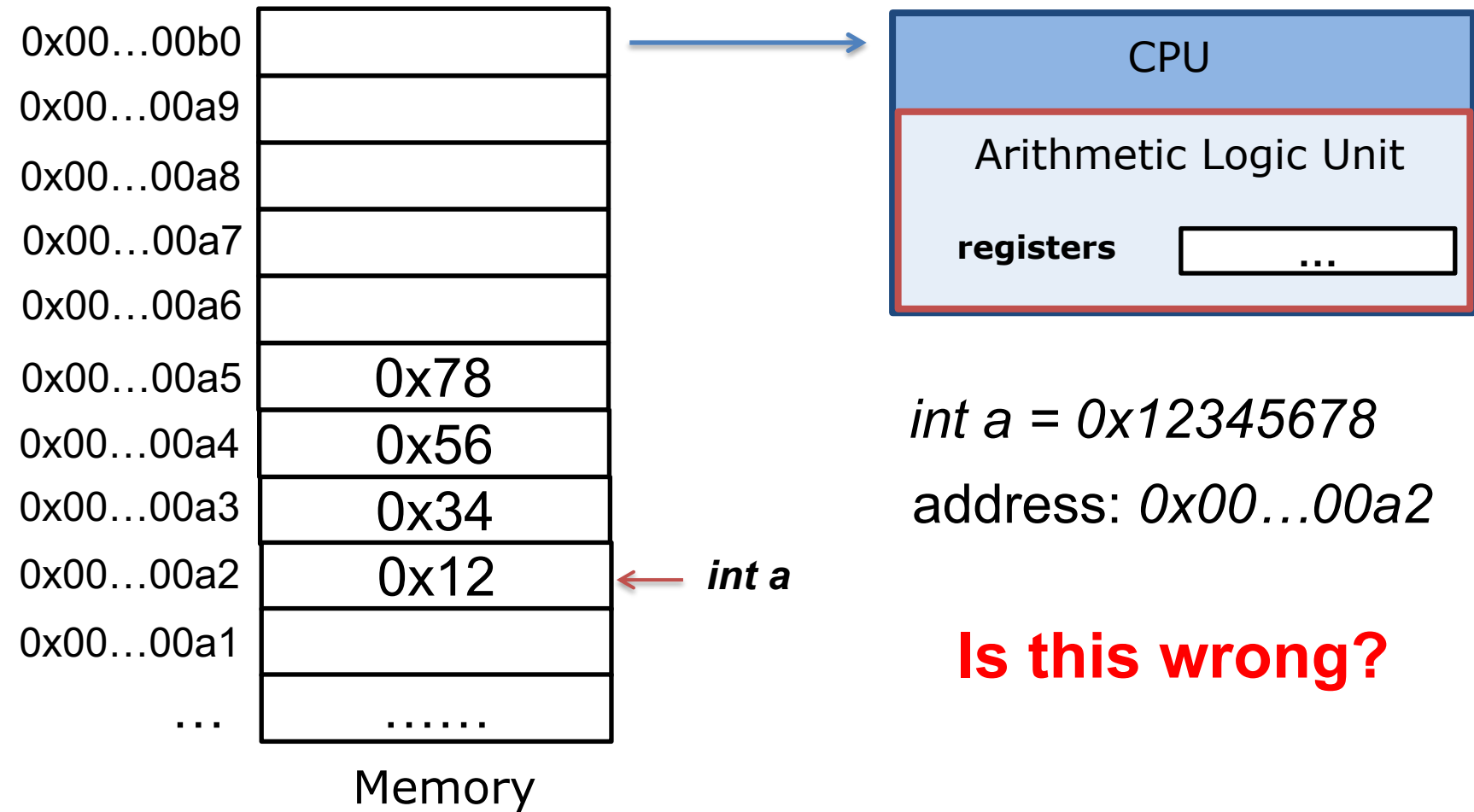
# Advantages of Little Endian



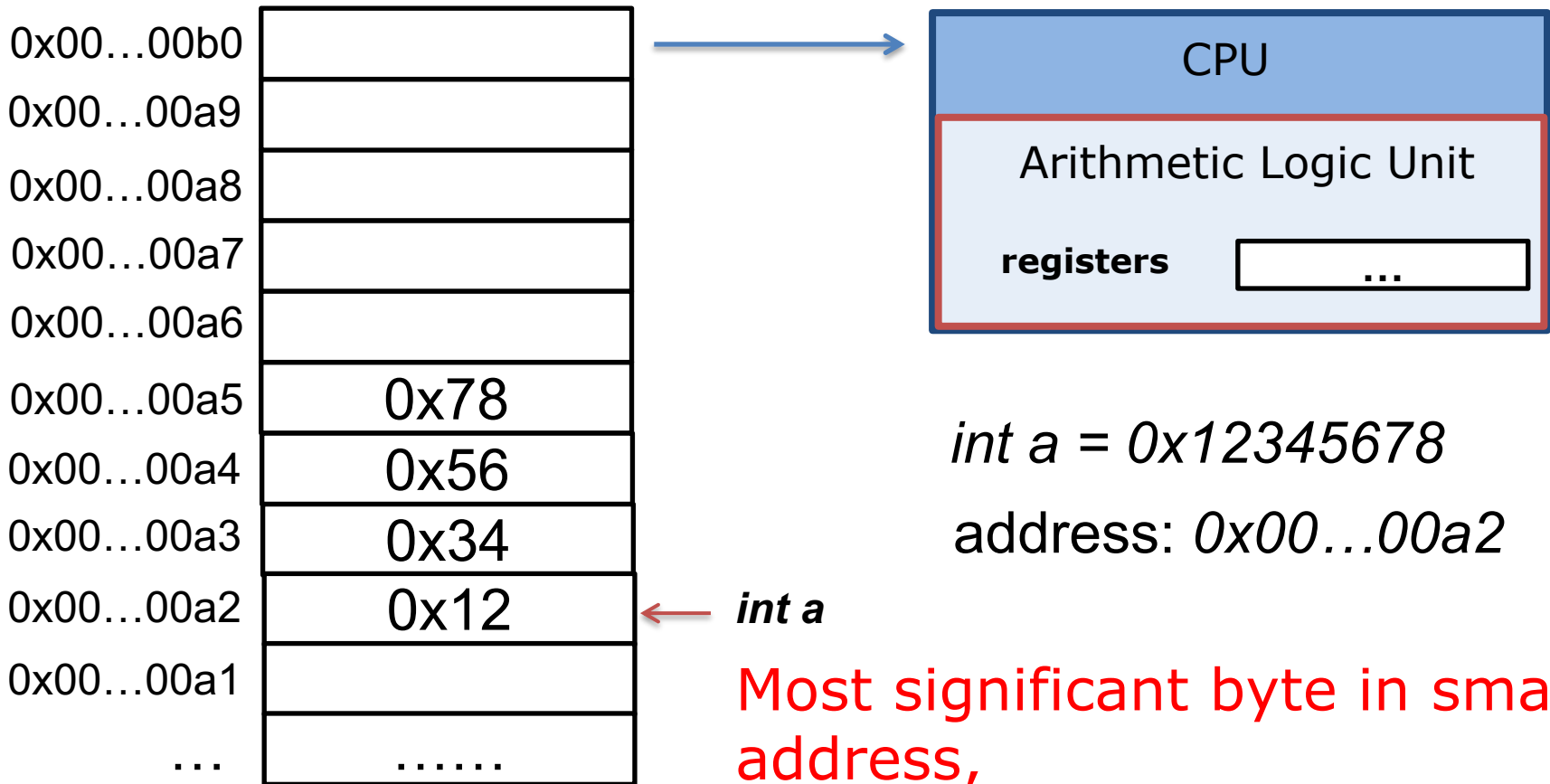
# Memory layout – Intuition



# Memory layout – Intuition



# Memory layout – Big Endian



Most significant byte in smallest address,  
e.g, ARM architecture >v3 (cellphones, ipads)



# Advantages of Big Endian

1. Easy to read
2. Test whether the number is positive or negative by looking at the byte at offset zero.